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Precalculus
Purpose: In this problem set, you will practice building new functions by transformations of old functions and identifying the parent function of a transformed function.

1. The graph of the function $f(x)$ is given on the coordinate axes below. For each transformation of $f$ below, draw the transformed graph. Make sure to set the scales on the axes in your solutions.

(a) $y=2 f(x)$

(d) $y=-2 f(x)$

(b) $y=-f(x-1)$

(e) $y=\frac{1}{3} f(x)$

(c) $y=f(-x)$

(f) $y=f(x)+2$

2. Fill in all of the blanks in the table below for which you have sufficient information. If you do not have sufficient information, write $N$.

| $x$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 3 | -1 | -4 | -6 | 0 | -3 | 32 |
| $f(-x)$ |  |  |  |  |  |  |  |
| $-f(x)$ |  |  |  |  |  |  |  |
| $f(x)-2$ |  |  |  |  |  |  |  |
| $f(x-2)$ |  |  |  |  |  |  |  |
| $f(x)+2$ |  |  |  |  |  |  |  |
| $2 f(x)$ |  |  |  |  |  |  |  |
| $-1 / 3 f(x)$ |  |  |  |  |  |  |  |

3. Describe the transformations required to transform the function $f$ into the function $g$. Remember that order matters! Check your work by starting with the formula for $f$ and performing each transformation at a time to see if you get to the formula for $g$.
(a) $f(x)=\sqrt{x}, g(x)=-3 \sqrt{x}-1$
(b) $f(x)=x^{3}, g(x)=(2 x+4)^{3}$
4. Find a partner and pick a toolkit function. For each sequence of function transformations below, perform the transformation your toolkit function algebraically and graphically.

Toolkit Function: $f(x)=$
(a) Compress horizontally by a factor of 2 Shift left 3 units

(c) Compress horizontally by a factor of $1 / 2$ Shift left 3 units

(b) Stretch horizontally by a factor of 2 Shift up 3 units Shift right 1 unit

(d) Compress vertically by a factor of 3
Reflect across the $x$-axis
Translate right 2 units


